ON THE DYNAMICAL PRINCIPLES OF THE MOTION OF VELOCIPEDES.

By W. J. MACQUORN RANKINE, C.E., LL.D., F.R.S.

By W. J. Macquorn Rankine, C.E., LL.D., F.R.S. (Concluded from page 163). In calculating the whole work done on a given journey the following principles are to be observed:—Calculate by Equation 18 the vertical ascent equivalent to the distance on a level; then, if none of the descending gradients are steeper than the rate of inclination expressed by the coefficient of resistance, take the actual difference of level of the two ends of the journey, multiply it by the ratio (1+b), in which the gross weight exceeds the weight of the rider; the product is to be added to or subtracted from the ascent previously computed, according as the difference of level is an ascent or a descent, and the result will be the height of a vertical ladder which is equivalent to the actual journey.

height of a vertical ladder which is equivalently incorrey.

The same mode of calculation would be applicable to all gradients, if the velocipede could safely be allowed to become freely accelerated on steep descents, so as to acquire a store of energy available for surmounting ascents. But if the brake is to be used, so as to prevent acceleration, the calculation is to be modified as follows:—When a descending gradient occurs in which i is greater than f, calculate what the depth of descent would have been in the same distance if i had been equal to f; in other words, multiply the actual depth of descent by \(\frac{\pi}{2} \), and use the product instead

of the actual descent in calculating a virtual or effective value of the difference of level of the ends of the journey. Another way of stating this is as follows:—When a descending gradient i occurs greater than f, multiply the depth of descent on the gradient by $1 - \frac{f}{\epsilon}$, and consider

the product as an ascent, to be combined with the actual difference of level of the ends of the journey, in order to allow for the loss of the energy that might have been acquired by acceleration on the steep descending gradient. In algebraical symbols, let R, be the resistance on a level; and let z denote, if positive, the total ascent, and, if negative, the total descent during the journey, modified, if necessary, in the manner already described, to allow for the loss of energy due to the use of the brake on steep descents; then the work done is equivalent to that of raising the weight of the rider vertically upwards to the following height:—

Rac + (1 + b) W s

$$\frac{R_0 x + (1+b) W s}{W} = (1+b) (fx+s); \quad . \quad (20)$$

in the first member of which R, denotes the resistance on a level. An ascent may be reduced to an equivalent additional distance, and a descent (with due deduction for the use of the brake) to an equivalent saving of distance, by

use of the brake) to an equivalent saving of distance, by dividing by f.

24. Driving Pressure.—While the velocipede advances through a distance equal to half a revolution of the driving wheel the pressure of the foot of the rider is exerted through a distance equal to twice the crank-arm. Hence the pressure of the foot of the rider must be as many times greater than the total resistance as half the circumference of the driving wheel is greater than twice the crank-arm. In symbols, let c be the crank-arm; d the dismeter of the driving wheel, so that m d is its circumference; P the pressure of the foot on the stirrup; then

of the foot on the stirrup; then
$$P = \frac{\pi d R}{4 c} = \frac{\pi d}{4 c} (f \pm i) (1 + b) W; \quad . \quad (21)$$

nd the ratio of the pressure required to the weight of the

$$\frac{P}{W} = \frac{\pi d}{4 c} (f \pm i) (1 + b) (22)$$

Ordinary values of the ratio $\frac{\pi}{4c}$ range from 4 to 8; being often capable of adjustment by shifting the position of the treadles in the cranks. As an example, let us suppose this ratio to be 5; let the roadway be level, and, as before, let $f(1+b) = \frac{1}{40}$. Then we have $\frac{P}{W} = \frac{1}{8}$; or the pressure required is one sightly of the width of the sightly state.

required is one-eighth of the weight of the rider.

Another calculation which may be made is of the following kind: Assuming that the rider is able to exert a pressure bearing a given ratio to his weight, what rate of ascent will this enable him to surmount? The answer is given by the following equation: following equa

$$i = \frac{4cP}{(1+b)\pi dW} - f \dots \qquad (23)$$

For example, the data being the same as before, let us ssume that the rider is able to exert a pressure equal to half his weight, so that $\frac{P}{W} = \frac{1}{2}$; then we have

 $i = \frac{1}{1.25 \times 5 \times 2} - 0.02 = 0.08 - 0.02 = 0.06 = 1 \text{ in 16 nearly.}$ With a pressure equal to his whole weight we should have i = 0.16 - 0.02 = 0.14 = 1 in 7 nearly.

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25. Day's Work of the Rider.—It has been ascertained by experiment that a man of ordinary strength and activity, climbing a vertical ladder, is able to ascend for eight hours per day with an average speed of about half a foot (or 1524 millimetres) per second; which gives as his day's work the raising of his own weight to a height of 14,400t., or nearly 4400 metres. This, however, is known to be the most favourable way in which the muscular power of the legs can be exerted, the pressure of the foot being at all times equal to the whole weight of the man. During less favourable modes of exerting the legs, and especially when the pressure of the foot parallel to the direction of motion is much less than the weight of the man, a much smaller amount of daily work is to be expected. Accordingly, we find that the work of a velocipade journey of sixty miles on a level road is equivalent to lifting the rider 7920ts, or only about 0.55 of the day's work of vertical climbing.

Further experiments are necessary before any conclusion can be arrived at as to the utmost daily work to be ex-

pected from velocipede riders when the powers of the vehicle have been fully developed. A day's work equal to that of vertical climbing would correspond to a journey of about 110 miles on a smooth level road.

A rough comparison, however, may be drawn between velocipede-riding and walking, in the following way. Suppose we assume that a man who can ride 60 miles per day on a velocipede on a smooth level road is able to walk 30 miles per day. The length of the day's journey in walking will not be lessened to any material extent by the occurrence of any degree of roughness or steepness that it is consistent, with using the velocipede at all. Hence that degree of one-fortist of the weight, or one-twentieth instead of one-fortist of the weight of the rider, brings down velocipede-riding to an equality with walking; and any greater day advantage.

The same method may be applied to other numerical data. Suppose, for example, that it should be accertained that a man who can walk 30 miles per day is able to ride; the degree of roughness or of steepness gives walking the advantage.

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KNAGG'S PROCESS OF CANE SUGAR MAKING.

In our impression of November the 8th, 1867, we gave a detailed description, illustrated by woodcuta, of Mr. Knagg's patent process of clarifying cane juice, and subsequent evaporation and granulation; we also mentioned that the whole process had been exhibited in operation at the works of Messrs. Easton, Amos, and Anderson, at Erith in the presence of a large number of gentlemen interested in the sugar trade, and that the opinion formed by all present was extremely favourable to the new process. We have since watched the colonial papers with some interest, to ascertain if the invention was making head, and if the results obtained under a tropical sun, and subject to all local difficulties, were as favourable as those we ourselves witnessed at Erith, and ventured to anticipate for the apparatus when put into actual use. The first portion of Mr. Knagg's invention, viz., the defecation and clarifying by means of sulphurous acid gas and permanganate of potash, has now been tried in Demerara, Trinidad, Jamaica, and is in process of trial at Bribabne; in every case the most complete success has been achieved. For instance, to quote from the Trinidad Chronicle of Feb. 28th, 1868, from a report signed by no less than eleven planters:

The process is free from complication and efficacious, and within the working power of any man of ordinary capacity. The juice is thoroughly clarified, and enters the coppers so pure that skimming is almost dispensed with-so much so that were it entirely omitted, the sugar would be far cleaner than any amount of manipulation can make it under the ordinary process. The juice is greatly decolourised, entering the copper-wall of the coloury of pale brandy and water, and as clear. Again Messra. Bernard and Messra. John Spiers and Co., state "the conomy and advantage of your process, as far as we can now judga, it as a follows:—(1). Two clarifiers being required where four are now used; (2), the ignor after being defeased by the minghurous gas, comes fro

outley required.

The complete apparatus, the trial of which we witnessed at Erith, has as yet only been erected on the Bushy Park estate in Jamaica—but we see by the Gleaver of Kingston, Jamaics, July 9th, 1869, that a committee of fifteen planters have reported very favourably, especially of the evaporator, of which they say: "That the evaporator is decidedly the most effectual, economical, and expeditious mode of evaporating cane juice we have seen or heard of, and as a proof we give the following results:—

The cane juice from the clarifers on entering the evaporator stood at \$1 deg. Beaums, and in see minutes came out at 30 deg.

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stod at 8½ deg. Beaums, and in see measures came out at 30 deg. to 35 deg.

Wegather from the same paper that Mr. Knagg's invention is attracting considerable attention in the colony, so much so that the Governor and the Commander of the Forces, have honoured a public exhibition of the process with their presence; and there can be no doubt that if Mr. Knagg's invention realises the expectations which those who have seen it in operation entertain, it will have a very important effect upon the prosperity of our sugar-growing colonies, by improving the quality of the produce, and reducing to a minimum the amount of skilled, or, indeed, any labour required. We have selected the present moment for again drawing the attention of our readers to this subject, because we, think that, during the existing disturbances in Cube, our colonies, with proper appliances, may become the first sugar producing communities in the world; but to do so, the islands must not, as the Governor of Jamaica is reported to have remarked, "stick in the mud and do things in the way their grandfathers did them, but copy the energy and scientific skill of those who have succeeded in making the despined beet-root a formidable rival; and we do not see that they can make a better beginning than by adopting

the despised beet-root a formidable rival; and we do not see that they can make a better beginning than by adopting the invention of one of their own people."

If these considerations have force in connection with the islands, they apply still more completely in the case of the mainland colonies. Demerara and Berbice, with large vacuum pan estates, and ample supplies of water for working them, should stand paramount insugar production and in sugars of high quality; but these facilities, great as they are, may be immeasurably improved by the general introduction of an improved clarification, such as the system now under consideration embraces, and notably by the

by this system.

Nothing can be stronger than this; and the system of machinery involved offers every inducement to the production of Muscavado and other high class sugars of such colour and quantity as would command the best prices, short of bringing them into the classes where our present somewhat anomalous Customs' restrictions would operate to their prejudice.

WORKING MEN'S CLUB AND INSTITUTE UNION. —VISIT TO CROSSNESS.

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WORKING MEN'S CLUB AND INSTITUTE UNION.
—VISIT TO CROSSNESS.

This council of the Working Men's Club and Institute Union wisely determined some times since to arrange a series of visits by the members of the Union to public buildings and important and the Union of the Union to public buildings and important series of these wists have already come off—to the Holborn Valley Improvement, St. Thomas's Homital, Blackfriare Bridge, the Metropolitan sewage outfall at Orosanes. The most recent visit of the series—which took place a few days ago—was to the metropolitan sewage outfall at Orosanes. The visit was intended to have included an inspection of the northern outfall at Barking case and the metropolitan in the series—which took place a few days ago—was to the metropolitan in any be left out of consideration in our secount of the visit of the series as well as the control of the visit of these visits as likely to exercise an important influence in connection with the technical education of the working men who may join the excursion. The policy of the council is to obtain for each visit the services of a "guide, philosopher, and friend" to the excursions the whole of the works while the plan and character of the works visited. In the visit to Crosness Mr. Edward Hall, F.S.A., was the guide and expositor. On the evening prior to the visit.—Friday last—Mr. Hall delivered a lecture, shundantly illustrated with dargrams, by favour of Mr. Bassigette, on the metropolitan sewage system, in the Lecture Being down the river on Saturday afternoon, and our own inquiries and inspection, we complete the following account of the works and the visit.

The lacture on Friday evening was numerously attended. It is proverbially dangearous to judge from appearances, and unsafe to consulted from them condiently. We resture to this, notwith standing, that if the sudience at the lecture and the visitors to Crosness on the following afternoon were, for the greater p