Using a technique which he calls the Boltzman Hamel method, in 1978 Gobas presented a linearized set of equations very similar in form to Neimark and Fufaev [1967]. Gobas’ equations, (1.4) in his paper, incorporate the forward acceleration of the bicycle, \( \ddot{V} \). Setting \( V \) terms to zero and comparing, we think the lean equation may be correct, but in the steer equation the coefficient to the \( \chi_r \) term seems to be in disagreement with the equations in our Chapter III. The variable \( b \) is not defined in the paper but we suspect that it is equivalent to our \( \nu \).

Gobas refers to Neimark and Fufaev, but does not compare equations.

Adiele, 1979

In his 1979 Master’s thesis Adiele, who was focusing on design optimization and performance evaluation of two-wheeled vehicles, derived nonlinear equations of motion for the Basic bicycle with tire side slip using Kane’s method of generalized active and inertia forces.

His equations, representing lateral motion, lean, steer, and yaw (in that order) are present in matrix form on pages 22-24 of his thesis. His variable \( V \) is our \( \dot{X}_r \), \( \lambda \) is our \( \chi_r \), \( \theta \) is our \( \psi \), and \( r \) is our \( \theta_r \). Because his equations resembled Sharp’s [1971] four equations, we expanded Adiele’s matrix, linearized his equations for small values of \( \lambda \) and \( \theta \), and compared them to the equations in Sharp’s [1971] Appendix I.

The results show that Adiele’s equations are in error, missing several terms